## Worksheet 5.1

1) Calculate the centripetal force acting on a 925 kg car as it rounds an unbanked curve with a radius of 75 m at a speed of $22 \mathrm{~m} / \mathrm{s}$.
2) A small plane makes a complete circle with a radius of 3282 m in 2.0 min . What is the centripetal acceleration of the plane?
3) A car with a mass of 833 kg rounds an unbanked curve in the road at a speed of $28.0 \mathrm{~m} / \mathrm{s}$. If the radius of the curve is 105 m , what is the average centripetal force exerted on the car?
( $6.2 \times 10^{3} \mathrm{~N}$ )
4) An amusement park ride has a radius of 2.8 m . If the time of one revolution of a rider is 0.98 s , what is the speed of the rider? ( $18 \mathrm{~m} / \mathrm{s}$ )
5) An electron ( $m=9.11 \times 10^{-31} \mathrm{~kg}$ ) moves in a circle whose radius is 2.00 x $10^{-2} \mathrm{~m}$. If the force acting on the electron is $4.60 \times 10^{-14} \mathrm{~N}$, what is its speed? ( $3.18 \times 10^{7} \mathrm{~m} / \mathrm{s}$ )
6) A 925 kg car rounds an unbanked curve at a speed of $25 \mathrm{~m} / \mathrm{s}$. If the radius of the curve is 72 m , what is the minimum coefficient of friction between the car and the road required so that the car does not skid?
7) A $2.7 \times 10^{3} \mathrm{~kg}$ satellite orbits the Earth at a distance of $1.8 \times 10^{7} \mathrm{~m}$ from the Earth's centre at a speed of $4.7 \times 10^{3} \mathrm{~m} / \mathrm{s}$. What force does the Earth exert on the satellite?
$\left(3.3 \times 10^{3} \mathrm{~N}\right)$
8) A string can withstand a force of 135 N before breaking. A 2.0 kg mass is tied to the string and whirled in a horizontal circle with a radius of 1.10 m . What is the maximum speed that the mass can be whirled at before the string breaks?
9) A 932 kg car is traveling around an unbanked turn with a radius of 82 m . What is the maximum speed that this car can round this curve before skidding:
a) if the coefficient of friction is 0.95 ?
b) if the coefficient of friction is 0.40 ?

## Worksheet 5.2

1) You are riding your bike on a track that forms a vertical circular loop. If the diameter of the loop is 10.0 m , what is the minimum speed required for you to make it around the loop?
( $7.00 \mathrm{~m} / \mathrm{s}$ )
2) You are swinging a bucket of water in a vertical circle. Assuming that the radius of the rotation of the water is 0.95 m , what is the minimum velocity of the bucket at the top of its swing if the water is not to spill?
( $3.1 \mathrm{~m} / \mathrm{s}$ )
3) A student has a weight of 655 N . While riding a roller coaster they seem to weigh $1.96 \times 10^{3} \mathrm{~N}$ at the bottom of a dip that has a radius of 18.0 m . What is the speed of the roller coater at this point?
( $18.7 \mathrm{~m} / \mathrm{s}$ )
4) A string requires 186 N of force to break. A 1.50 kg mass is tied to the string and whirled in a vertical circle with a radius of 1.90 m . What is the maximum speed that this mass can be whirled at without breaking the string?
5) A 2.2 kg object is whirled in a vertical circle whose radius is 1.0 m . If the time of one revolution is 0.97 s , what is the tension in the string (assume uniform speed)
a) at the top?
b) at the bottom?
6) A 915 kg car goes over a hill of circular arc. If the radius of the curve is 43 m , how fast can the car travel without leaving the road at the top of the arc?
7) What is the maximum speed for a car rounding a 125 m curve on a highway under very icy (no friction) conditions if the banking angle is $20.0^{\circ}$.
( $21.1 \mathrm{~m} / \mathrm{s}$ )
Yowsers!) An airplane traveling at a speed of $115 \mathrm{~m} / \mathrm{s}$ makes a complete horizontal turn in 2 minutes. What is the banking angle?
( $31.6^{\circ}$ to the horizontal))

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\mathrm{m}_{\text {Earth }}=5.98 \times 10^{24} \mathrm{~kg} \quad \mathrm{~m}_{\text {Moon }}=7.35 \times 10^{22} \mathrm{~kg}
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## Worksheet 5.3

1) Two students are sitting 1.50 m apart. One student has a mass of 70.0 kg and the other has a mass of 52.0 kg . What is the gravitational force between them?
( $1.08 \times 10-{ }^{-7} \mathrm{~N}$ )
2) What gravitational force does the moon produce on the Earth if their centers are $3.84 \times 10^{8} \mathrm{~m}$ apart?
(1.99x10 $0^{20} \mathrm{~N}$ )
3) if the gravitational force between two objects of equal mass is $2.30 \times 10-8$ N when the objects are 10.0 m apart what is the mass of each object?
(186 kg)
4) Calculate the gravitational force on a $6.50 \times 10^{2} \mathrm{~kg}$ spacecraft that is $4.15 \times 10^{6} \mathrm{~m}$ above the surface of the Earth.
$\left(2.34 \times 10^{3} \mathrm{~N}\right)$
5) The gravitational force between two objects that are $2.1 \times 10^{-1} \mathrm{~m}$ apart is $3.2 \times 10^{-6} \mathrm{~N}$. If the mass of one object is 55 kg , what is the mass of the other object?
( 38 kg )
6) If two objects, each with a mass of 200 kg , produce a gravitational force of $3.7 \times 10^{-6} \mathrm{~N}$, what is the distance between them?
( 0.85 m )
7) What is the gravitational force on a 70.0 kg object standing on the Earth’s surface?
( 686 N )
8) Three 10.0 kg objects are placed in a straight line $5.00 \times 10-1 \mathrm{~m}$ apart. What is the net gravitational force on the center object due to the other two objects?
9) Three objects A, B, and C are placed 0.50 m apart along a straight line. A and $B$ have masses of 10.0 kg and C has a mass of 15.0 kg , what is the net gravitational force on B due to A and C ?

10) The force of gravity between two small masses A and B when placed very near each other is $3.24 \times 10^{-7} \mathrm{~N}$. What will the force between these objects be if both of their masses are doubled and the distance between them is tripled?

## Worksheet 5.4

1) Calculate the gravitational field strength on the surface of Mars. Mars has a radius of $3.43 \times 10^{6} \mathrm{~m}$ and a mass of $6.37 \times 10^{23} \mathrm{~kg}$.
( $3.61 \mathrm{~N} / \mathrm{kg}$ )
2) At what distance from Earth's surface is the acceleration due to gravity $7.33 \mathrm{~m} / \mathrm{s}^{2}$ ?
( $9.97 \times 10^{5} \mathrm{~m}$ )
3) On the surface of Planet $X$ an object has a mass of 22.5 kg and a weighs 63.5 N . What is the gravitational field strength on the surface?
4) On the surface of Planet $Y$, which has a mass of $4.83 \times 10^{24} \mathrm{~kg}$, a 30.0 kg object weighs 50.0 N . What is the radius of the planet? ( $1.39 \times 10^{7} \mathrm{~m}$ )

## Worksheet 5.5

5) What is the gravitational potential energy (relative to infinite) of a $5.00 \times 10^{3} \mathrm{~kg}$ satellite that is in orbit with a radius of $9.90 \times 10^{6} \mathrm{~m}$ around the Earth?
$\left(-2.0 \times 10^{11} \mathrm{~J}\right)$
6) How much work is done against gravity in lifting the satellite in problem \#5 to its orbital height?
( $1.11 \times 10^{11} \mathrm{~J}$ )
7) A 1750 kg meteorite is 15000 m above the surface of the moon, heading directly towards the moon at $1.00 \times 10^{3} \mathrm{~m} / \mathrm{s}$. What is its speed on impact?
( $1.02 \times 10^{3} \mathrm{~m} / \mathrm{s}$ )
8) What is the gravitational potential energy of a 10.0 kg object when it is sitting on Earth's surface?
$\left(-6.25 \times 10^{8} \mathrm{~J}\right)$
9) What is the escape velocity of a 1300 kg shuttle taking off from the moon?
$\left(2.37 \times 10^{3} \mathrm{~m} / \mathrm{s}\right)$
10) What is the mass of a planet that has an escape speed of $9.0 \times 10^{3} \mathrm{~m} / \mathrm{s}$ and a radius of $7.2 \times 10^{6} \mathrm{~m}$ ?
$\left(4.37 \times 10^{24} \mathrm{~kg}\right)$
11) A 12500 kg satellite is in orbit at an altitude of $3.60 \times 10^{6} \mathrm{~m}$. What is its total energy?
HINT: Total Energy $=\mathrm{E}_{\mathrm{p}}+\mathrm{E}_{\mathrm{k}}$
